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受遮挡贝塞尔-高斯光束在湍流大气传输的 M² 因子

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摘要:为了研究受遮挡贝塞尔-高斯光束在湍流大气中传输时质量因子的特性,基于拓展的惠更斯-菲涅耳原理和 维格纳分布函数的二阶矩定义,经理论推导得出受遮挡贝塞尔-高斯光束的解析表达式,并进行了相应的数值计算。结 果表明,当遮挡物尺寸不大于0.4 倍的腰宽时,受遮挡贝塞尔-高斯光束在湍流大气中的传输质量因子随传播距离、湍流 大气结构常数的增大而增大,随着湍流内标量、光束拓扑荷数的增大而减小。在相同条件下,光束的传输质量因子随着 遮挡物尺寸的增大而增大。所得结论对实际激光传输和自由空间光通信有一定的参考价值。

关键词: 大气与海洋光学; M² 因子; 拓展的惠更斯-菲涅耳原理; 贝塞尔-高斯光束 中图分类号: TN012 文献标志码: A doi:10.7510/jgjs.issn.1001-3806.2018.03.026

M^2 factor of disturbed Bessel-Gaussian beam propagating in turbulent atmosphere

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Abstract: In order to study the propagation properties of the disturbed Bessel-Gaussian beam in turbulent atmosphere, based on the extended Huygens-Fresnel principle and the second-order moments of the Wigner distribution function, the formulas of M^2 factor for the disturbed Bessel-Gaussian beam were derived by theoretical calculation analysis, and the corresponding numerical calculation was carried out. The results show that, when the size of obstruction is not more than 0.4 times of beam width, the propagation factor of Bessel-Gaussian beam in turbulent atmosphere would increase with the increasing of the propagation distance and atmospheric structure constant, and decrease with the increasing of the inner scale of turbulence and topological charge indexes. Under the same condition, the propagation factor of Bessel-Gaussian beam in turbulent atmosphere increases with the increase of the size of obstruction. These results have certain reference value in free space optical communication and actual laser transmission.

Key words: atmospheric and ocean optics; M^2 factor; expanded Huygens-Fresnel principle; Bessel-Gaussian beam

引 言

激光束在光学成像、激光遥感、光互联和自由空间 光通信等方面有大量的应用,使得激光束在大气湍流 中的研究受到国内外学者的广泛关注^[16]。但是由于 大气湍流的存在,激光束在大气中传输时不可避免地 受到湍流的影响,发生光束漂移^[79]、光束质量^[10]、强 度^[11-12]、相干性^[13]和偏振性^[14]变化等一系列的湍流 效应,使得激光束的光束质量大大降低,因此寻找合适 的激光束以减小大气湍流对光束的影响是众多学者一 直努力的方向。参考文献[13]中研究了部分相干高 斯-谢尔光束在大气湍流中的传输特性,发现一定条件 下部分相干光与完全相干光相比,它受大气湍流的影 响更小。参考文献[14]中提出矢量涡旋光束在大气 中传输时,受到湍流的干扰相对小。自 1987 年 DURNIN 首次提出了近似无衍射光束的概念并在实验 中产生了这种新型的光束^[15]以来,这种新型的光束便 引起了众多学者的兴趣。1996 年研究人员发现当贝 塞尔光束的中心光斑被遮挡后,经过很小的一段距离 就可以恢复的自愈合特性^[16-19]。参考文献[20]中从

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理论上推导了贝塞尔光束在大气湍流中的光束漂移模型,计算了不同湍流强度下高阶贝塞尔光束的光束漂移,结果表明,在相同的大气湍流条件下,高阶贝塞尔光束受大气湍流的影响较小,因此,研究贝塞尔光束在大气湍流中的传输性质对于自由空间光通信等诸多方面有很重要的意义。鉴于此,本文中基于拓展的惠更斯-菲涅耳原理和维格纳分布函数的二阶矩定义理论上推导了受遮挡贝塞尔-高斯光束在大气湍流中的质量因子解析式,进行相应的数值计算,分析了湍流大气结构常数、湍流内标量、遮挡物尺寸和束腰宽度对受遮挡贝塞尔-高斯光束的质量因子的影响。

1 理论推导

在柱坐标下,参考文献[3]中给出了贝塞尔-高斯 光束在源平面的(z=0)的电场强度分布表达式,在光 束的中心加一个障碍物即高斯吸收函数^[17],则其在源 平面的电场强度分布函数可以表示为:

$$E_{0}(\rho,\varphi,0) = J_{m}\left(\frac{R}{w_{0}^{2}}\rho\right)\exp\left(-\frac{\rho^{2}}{w_{0}^{2}}\right) \times \exp\left(-im\varphi\right)\left[1 - \exp\left(-\frac{\rho^{2}}{R_{0}^{2}}\right)\right]$$
(1)

源平面上交叉谱密度函数可以表示为:

$$W(\rho_{1},\rho_{2},0) = J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{1}\right)J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{2}\right) \times \\ \exp\left[-\frac{\rho_{1}^{2}+\rho_{2}^{2}}{w_{0}^{2}}-im(\varphi_{1}-\varphi_{2})\right]+J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{1}\right) \times \\ J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{2}\right)\exp\left[-\frac{\rho_{1}^{2}+\rho_{2}^{2}}{w_{1}^{2}}-im(\varphi_{1}-\varphi_{2})\right] - \\ J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{1}\right)J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{2}\right) \times \\ \exp\left[-\frac{\rho_{1}^{2}}{w_{0}^{2}}-\frac{\rho_{2}^{2}}{w_{1}^{2}}-im(\varphi_{1}-\varphi_{2})\right] - \\ J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{1}\right)J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{2}\right) \times \\ \exp\left[-\frac{\rho_{1}^{2}}{w_{1}^{2}}-\frac{\rho_{2}^{2}}{w_{0}^{2}}-im(\varphi_{1}-\varphi_{2})\right] - \\ \left[-\frac{\rho_{1}^{2}}{w_{1}^{2}}-\frac{\rho_{2}^{2}}{w_{0}^{2}}-im(\varphi_{1}-\varphi_{2})\right] \right]$$
(2)

式中, J_m 表示 m 阶第 1 类贝塞函数, w₀ 为基模高斯光 束的束腰宽度, 参量 $R = kw_0^2 \sin\varphi$, φ 表示在傍轴上理 想贝塞尔场的锥角, $k = \frac{2\pi}{\lambda}$ 表示波数, λ 为光束的波长, R_0 为遮挡物半径, $\rho_i = (\rho_{xi}, \rho_{yi}) = (\rho_i \cos\varphi_i, \rho_i \sin\varphi_i)$ 表示 源平面中任意的两个点, φ 表示沿 z 方向的角, $w_1^2 = \frac{R_0^2 + w_0^2}{w_0^2 R_0^2}$ 。在(2)式中取:

$$W_{1}(\rho_{1},\rho_{2},0) = J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{1}\right)J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{2}\right) \times \exp\left[-\frac{\rho_{1}^{2}+\rho_{2}^{2}}{w_{0}^{2}}-im(\varphi_{1}-\varphi_{2})\right],$$

$$W_{2}(\rho_{1},\rho_{2},0) = J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{1}\right)J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{2}\right) \times \exp\left[-\frac{\rho_{1}^{2}+\rho_{2}^{2}}{w_{1}^{2}}-im(\varphi_{1}-\varphi_{2})\right],$$

$$W_{3}(\rho_{1},\rho_{2},0) = J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{1}\right)J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{2}\right) \times \exp\left[-\frac{\rho_{1}^{2}}{w_{0}^{2}}-\frac{\rho_{2}^{2}}{w_{1}^{2}}-im(\varphi_{1}-\varphi_{2})\right],$$

$$W_{4}(\rho_{1},\rho_{2},0) = J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{1}\right)J_{m}\left(\frac{R}{w_{0}^{2}}\rho_{2}\right) \times \exp\left[-\frac{\rho_{1}^{2}}{w_{1}^{2}}-\frac{\rho_{2}^{2}}{w_{0}^{2}}-im(\varphi_{1}-\varphi_{2})\right],$$

$$(3)$$

根据参考文献[5],可得 $W_1(\rho_1,\rho_2,0)$ 的表达式。 为简单起见,引入新的积分变量 $\rho = (\rho_1 + \rho_2)/2, \rho_d = \rho_1 - \rho_2,$ 可得: $W_{1\theta\theta'}(\rho_1,\rho_2,0) \Rightarrow W_{1\theta\theta'}(\rho,\rho_d,0)$ 。

$$w_{1\theta\theta'}(\rho,\rho_{\rm d},0) = \exp\left[-\frac{2\rho^{2}}{w_{0}^{2}} - \frac{\rho_{\rm d}^{2}}{2w_{0}^{2}} + i\left(\boldsymbol{Q}_{-}\cdot\rho + \frac{\boldsymbol{Q}_{+}\cdot\rho_{\rm d}}{2}\right)\right] \quad (4)$$

式中,2 维矢量 $Q_{\pm} = \frac{R}{w_0^2} (\cos\theta \pm \cos\theta', \sin\theta \pm \sin\theta'), \theta$ 和 θ' 是积分公式与贝塞尔函数之间转换引人的无关变量。

激光从源平面(z=0)出发,在湍流大气中传输时, 参考文献[14]中给出了光束在z平面的表达式,在此 引入新的积分变量 $r = \frac{r_1 + r_2}{2}, r_d = r_1 - r_2, 其中, r_1$ 和 r_2 表示接收面上任意的两个点,垂直于光束的传播方向,得:

$$\langle W_{1\theta\theta'}(\boldsymbol{r},\boldsymbol{r}_{d},z) \rangle = \left(\frac{1}{2\pi}\right)^{2} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} d^{2}\rho' d^{2}\boldsymbol{\kappa}_{d} \times \langle W_{1\theta\theta'}(\rho',\boldsymbol{r}_{d} + \frac{z}{k}\boldsymbol{\kappa}_{d},0) \rangle \times \exp\left[-i\boldsymbol{r}\cdot\boldsymbol{\kappa}_{d} + i\rho'\cdot\boldsymbol{\kappa}_{d} - H\left(\boldsymbol{r}_{d},\boldsymbol{r}_{d} + \frac{z}{k}\boldsymbol{\kappa}_{d},z\right)\right]$$
(5)

式中,**κ**_d 是空间频域的位置矢量,*H* 表示湍流影响。 对无关变量 *ρ*′进行积分并整合得到:

$$\langle W_{1\theta\theta'}(\boldsymbol{r},\boldsymbol{r}_{\mathrm{d}},z) \rangle = \frac{w_0^2}{8\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \exp(-\mathrm{i}\boldsymbol{r}\cdot\boldsymbol{\kappa}_{\mathrm{d}}) \times$$

$$\exp\left[-\frac{w_{0}^{2}\boldsymbol{Q}_{-}^{2}}{8}-\frac{1}{2w_{0}^{2}}\boldsymbol{r}_{d}^{2}+\frac{\mathrm{i}\boldsymbol{Q}_{+}}{2}\cdot\boldsymbol{r}_{d}-H\left(\boldsymbol{r}_{d},\boldsymbol{r}_{d}+\frac{z}{k}\boldsymbol{\kappa}_{d},z\right)\right]\times\\\exp\left[-\left(\frac{w_{0}^{2}}{8}+\frac{z^{2}}{2w_{0}^{2}k^{2}}\right)\boldsymbol{\kappa}_{d}^{2}+\left(\frac{\mathrm{i}\boldsymbol{Q}_{+}}{2k}-\frac{w_{0}^{2}\boldsymbol{Q}_{-}}{4}-\frac{z}{kw_{0}^{2}}\cdot\boldsymbol{r}_{d}\right)\cdot\boldsymbol{\kappa}_{d}\right]\mathrm{d}^{2}\boldsymbol{\kappa}_{d} \qquad (6)$$

受遮挡贝塞尔-高斯光束在大气湍流中传输时,其 维格纳分布函数可以表示为:

$$h(\boldsymbol{r},\boldsymbol{\varphi},z) = \int_{0}^{2\pi} \int_{0}^{2\pi} \mathrm{d}\theta \mathrm{d}\theta' \exp\left[-\mathrm{i}m(\theta-\theta')\right] h_{\theta\theta'}(\boldsymbol{r},\boldsymbol{\varphi},z) \quad (7)$$

其中,

$$h_{\theta\theta'}(\boldsymbol{r},\boldsymbol{\varphi},z) = \left(\frac{k}{2\pi}\right)^2 \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} W_{\theta\theta'}(\boldsymbol{r},\boldsymbol{r}_{\mathrm{d}},z) \times \exp(-\mathrm{i}\boldsymbol{k}\boldsymbol{r}_{\mathrm{d}}\cdot\boldsymbol{\varphi}) \,\mathrm{d}^2\boldsymbol{r}_{\mathrm{d}} = D \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \mathrm{d}^2\boldsymbol{r}_{\mathrm{d}} \,\mathrm{d}^2\boldsymbol{\kappa}_{\mathrm{d}}\Lambda_{\theta\theta'}(\boldsymbol{r}_{\mathrm{d}},\boldsymbol{\kappa}_{\mathrm{d}},z) \times \exp(-\mathrm{i}\boldsymbol{k}\boldsymbol{r}_{\mathrm{d}}\cdot\boldsymbol{\varphi} - \mathrm{i}\boldsymbol{\kappa}_{\mathrm{d}}\cdot\boldsymbol{r})$$
(8)

式中, $D = \frac{k^2 w_0^2}{8\pi^3}$, $\varphi = (\varphi_x, \varphi_y)$ 表示这个矢量沿 z 方向的 角, $k\varphi_x, k\varphi_y$ 分别表示沿 x 轴和 y 轴方向的波矢量分 量, $\Lambda_{\theta\theta'}$ 是引入的一个函数,是 $W_{1\theta\theta'}$ 对 ρ' 进行积分后取 得的一个函数。

由于维格纳分布函数的性质及(n₁ + n₁ + m₁ + m₂)阶矩定义^[10],可得:

$$\begin{split} \langle x^{2} + y^{2} \rangle_{1} &= f_{1} \Big[\exp(-\gamma_{1}) \operatorname{I}_{m}(\gamma_{1}) g_{1} + \\ \exp(-\gamma_{1}) \operatorname{I}_{m+1}(\gamma_{1}) \Big(\frac{R^{2} z^{2}}{4 w_{0}^{-4} k^{2}} \Big) + \exp(-\gamma_{1}) \times \\ \operatorname{I}_{m-1}(\gamma_{1}) \Big(\frac{R^{2} z^{2}}{4 w_{0}^{-4} k^{2}} \Big) + \exp(-\gamma_{1}) \operatorname{I}_{m+1}(\gamma_{1}) \Big(\frac{R^{2}}{16} \Big) + \\ &\exp(-\gamma_{1}) \operatorname{I}_{m-1}(\gamma_{1}) \Big(\frac{R^{2}}{16} \Big) \Big], \\ \langle x \varphi_{x} + y \varphi_{y} \rangle_{1} &= f_{1} \Big[\exp(-\gamma_{1}) \operatorname{I}_{m}(\gamma_{1}) j_{1} + \\ &\exp(-\gamma_{1}) \operatorname{I}_{m+1}(\gamma_{1}) \Big(\frac{R^{2} z}{4 w_{0}^{-4} k^{2}} \Big) + \\ &\exp(-\gamma_{1}) \operatorname{I}_{m-1}(\gamma_{1}) \Big(\frac{R^{2} z}{4 w_{0}^{-4} k^{2}} \Big) \Big], \\ \langle \varphi_{x}^{-2} + \varphi_{y}^{-2} \rangle_{1} &= f_{1} \frac{w_{0}^{-2}}{8 \pi} \Big[\exp(-\gamma_{1}) \operatorname{I}_{m}(\gamma_{1}) v_{1} + \\ &\exp(-\gamma_{1}) \operatorname{I}_{m+1}(\gamma_{1}) \Big(\frac{R^{2}}{4 w_{0}^{-4} k^{2}} \Big) + \end{split}$$

$$\exp(-\gamma_{1}) \mathbf{I}_{m-1}(\gamma_{1}) \left(\frac{R^{2}}{4w_{0}^{4}k^{2}}\right)$$
 (9)

式中, I_m 表示 m 阶修正的贝塞尔函数和。

$$\begin{cases} f_{1} = \frac{(2\pi)^{6} w_{0}^{2} D}{8\pi k^{2}} \\ \gamma_{1} = \frac{R^{2}}{4w_{0}^{2}} \\ g_{1} = \left(\frac{w_{0}^{2}}{2} + \frac{2z^{2}}{w_{0}^{2}k^{2}} + \frac{4\pi^{2}z^{3}T}{3} + \frac{R^{2}z^{2}}{2w_{0}^{4}k^{2}} - \frac{R^{2}}{8}\right) \\ j_{1} = \left(\frac{2z}{w_{0}^{2}k^{2}} + 2\pi^{2}z^{2}T + \frac{R^{2}z}{2w_{0}^{4}k^{2}}\right) \\ v_{1} = \left(\frac{2}{w_{0}^{2}k^{2}} + 4\pi^{2}zT + \frac{R^{2}}{2w_{0}^{4}k^{2}}\right) \end{cases}$$

$$(10)$$

式中,*T*是与空间功率谱函数相关的一个参量。同理 可以求出 $W_2(\rho_1,\rho_2,0), W_3(\rho_1,\rho_2,0), W_4(\rho_1,\rho_2,0)$ 的 参量组合。根据魏格纳分布函数的二阶矩理论,可以 分析光束束宽 $\langle x^2 + y^2 \rangle^{1/2}$ 和光束发散角 $\langle \varphi_x^2 + \varphi_y^2 \rangle^{1/2}$ 的变化规律,同时可以求出非零交叉项 $\langle x\varphi_x + y\varphi_y \rangle^{1/2}$, 由光束束宽,光束发散角和非零交叉项,受遮挡贝塞 尔-高斯光束的 M^2 因子为^[10,21]:

$$M^{2}(z) = k(\langle r^{2} \rangle + \langle \varphi^{2} \rangle - \langle r\varphi \rangle^{2})^{1/2} = k\{ [\langle x^{2} + y^{2} \rangle_{1} + \langle x^{2} + y^{2} \rangle_{2} + \langle x^{2} + y^{2} \rangle_{3} + \langle x^{2} + y^{2} \rangle_{4}] \times [\langle \varphi_{x}^{2} + \varphi_{y}^{2} \rangle_{1} + \langle \varphi_{x}^{2} + \varphi_{y}^{2} \rangle_{2} + \langle \varphi_{x}^{2} + \varphi_{y}^{2} \rangle_{3} + \langle \varphi_{x}^{2} + \varphi_{y}^{2} \rangle_{4}] - [\langle x\varphi_{x} + y\varphi_{y} \rangle_{1} + \langle x\varphi_{x} + y\varphi_{y} \rangle_{2} + \langle x\varphi_{x} + y\varphi_{y} \rangle_{3} + \langle x\varphi_{x} + y\varphi_{y} \rangle_{4}]^{2} \}^{1/2}$$
(11)

2 数值计算

(11)式是本文中的主要解析表达式,它可以方便 地研究受遮挡贝塞尔-高斯光束在大气湍流中的质量 因子,利用 MATHEMATIC 软件,相应数值计算结果见 下。

图 1 中给出了遮挡参量 t 不同时,不同拓扑荷数 n 所对应的归一化 M^2 因子的特性曲线($w_0 = 5$ mm, $\lambda = 632.8$ nm, $l_0 = 5$ mm, $R = 6w_0$)。遮挡物的半径 $R_0 = tw_0$, t 表示遮挡物大小与贝塞尔-高斯光束光斑大小的关 系。图 1 反映出当遮挡参量不变时,贝塞尔-高斯光束 归一化的 M^2 因子随着拓扑荷数的增大而减小;当拓 扑荷数不变时,随着遮挡参量的增大,贝塞尔-高斯光



Fig. 1 The normalized M^2 factor of Bessel-Gaussian beam with different topological charges and obstacle parameters

束归一化的 M² 因子也在增大。

图 2 中给出了遮挡参量不同时,不同光束腰宽对 归一化 M^2 因子的影响特性 ($n = 1, l_0 = 5$ mm, $\lambda = 632.8$ nm, $R = 6w_0, R_0 = tw_0, C_n^2 = 10^{-16}$ m^{-2/3})。计算 结果表明,当遮挡参量不变时,贝塞尔-高斯光束归一 化的 M^2 因子随着腰宽的增大而减小;当腰宽不变时, 随着遮挡参量的增大,贝塞尔-高斯光束归一化的 M^2 因子也在增大。

图 3 中计算了选择不同的遮挡参量和不同湍流内标量时,归一化 M^2 因子的变化规律($n = 1, w_0 = 5$ mm, $\lambda = 632.8$ nm, $R = 6w_0, R_0 = tw_0, C_n^2 = 10^{-16}$ m^{-2/3})。图



Fig. 2 The normalized M^2 factor of Bessel-Gaussian beam with different waist widths and obstacle parameters

3 反映出当遮挡参量不变时,贝塞尔-高斯光束归一化 的 M² 因子随着湍流内标量的增大而减小;当湍流内 标量不变时,随着遮挡参量的增大,贝塞尔-高斯光束 归一化的 M² 因子也在增大的规律。

当改变遮挡参量和湍流大气结构常数时,归一化 M^2 因子的变化曲线见图 4($n = 1, l_0 = 5 \text{ mm}, w_0 = 5 \text{ mm}, R = 6w_0, R_0 = tw_0, \lambda = 632.8 \text{ nm}$)。图 4 很明显反映出 当遮挡参量不变时,贝塞尔-高斯光束归一化的 M^2 因 子随着湍流大气结构常数的增大而增大;当湍流大气 结构常数不变时,贝塞尔-高斯光束归一化的 M^2 因子 随着遮挡参量的增大而增大的现象。



Fig. 3 The normalized M^2 factor of Bessel-Gaussian beam with different inner scales and obstacle parameters

3 结 论

基于拓展的惠更斯-菲涅耳原理和维格纳分布函数的二阶矩定义,理论推导了受遮挡贝塞尔-高斯光束 在湍流大气传输中 M² 因子的解析表达式,分析了遮 挡参量、传播距离、湍流内标量、束腰宽度和湍流结构 常数等参量对受限贝塞尔-高斯光束质量因子的影响。 数值计算和分析表明,当遮挡物的尺寸为零,即不加障 碍物时,其传输质量因子随传播距离、湍流大气结构常 数的增大而增大,随着腰宽、湍流内标量、光束拓扑荷 数的增大而减小,而当遮挡物尺寸不大于 0.4 倍的腰



Fig. 4 The normalized M^2 factor of Bessel-Gaussian beam with different structure constants and obstacle parameters

宽时,该光束的传输质量因子也呈现相同的变化规律, 但随着遮挡物尺寸的增大,贝塞尔-高斯光束需要自愈 合的距离更远,在大气湍流扰动下,其传输质量因子也 更大。

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